

1) If 70J of energy is available for every 30C of charge. What is the voltage?

Solⁿ $V = \frac{W}{Q}$

$$V = \frac{70}{30} = 2.33 \text{ volts}$$

2) 5C of charge flow passed through a given point in a wire in 2sec. How many Amperes of current is flowing?

Solⁿ $I = \frac{Q}{T} = \frac{5C}{2 \text{ sec}} = 2.5A$

3) What is the power in watts, if energy is 50J, used in 2.5sec.

Solⁿ $P = \frac{W}{T}$

$$P = \frac{50J}{2.5 \text{ sec}}$$

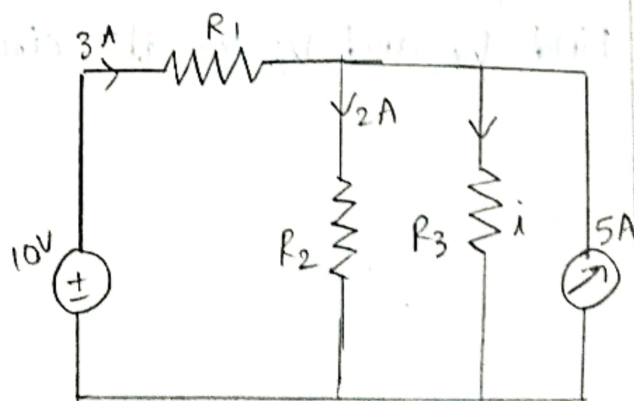
$$P = 20 \text{ watts.}$$

4) Compute the current through resistor R_3 . If it is known that voltage source supplies the current of 3A.

Solⁿ Apply KCL at Node A

$$3 + 5 + 2 + i$$

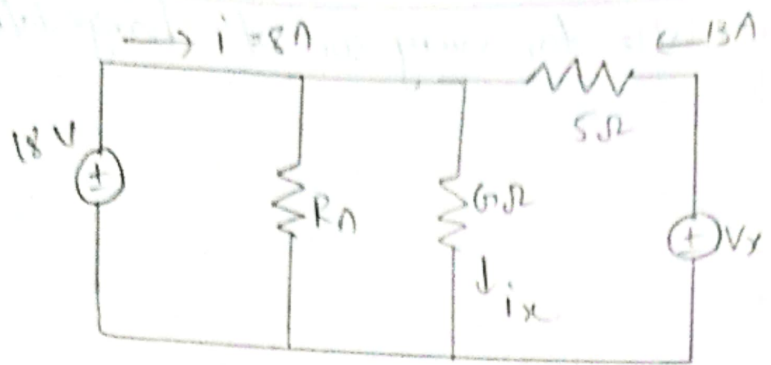
$$i = 6A$$



5) Count the number of branches and nodes in the given circuit, if $i_x = 3A$ & 18V source delivers 8A. What is the value of R_A .

Solⁿ Number of branches = 5

Number of nodes = 3



Given; $i_x = 3A$
 $V = 18V$

let 'i' be the current flowing through R_A .
 (Assume to be leaving from the node).

By KCL;

At node 1

$$8A + 13 = i + i_x$$

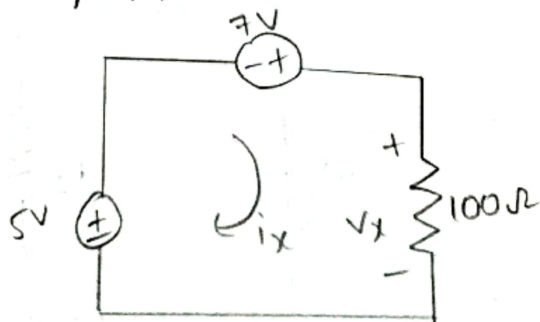
$$21 = i + i_x$$

$$i = 21 - 3$$

$$i = 18A$$

$$R_A = \frac{18}{i} = \frac{18}{18} = 1\Omega$$

6) Find V_x and V_i in the circuit.



Sol:

$$5V + 7V - V_x = 0$$

$$\boxed{V_x = 12V}$$

$$V = IR$$

$$I = \frac{V}{R} \Rightarrow I = \frac{12}{100} \Rightarrow I = 0.12A$$

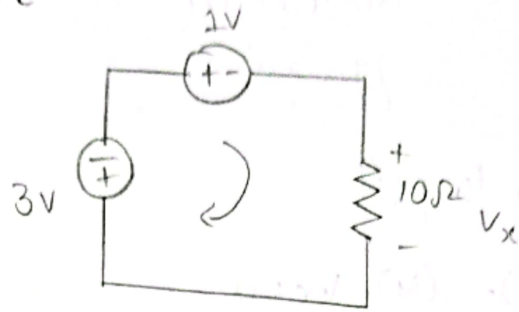
7) Find V_x and i_x in the circuit.

Sol: $3 + 1 = V_x$
 $V_x = -4V$

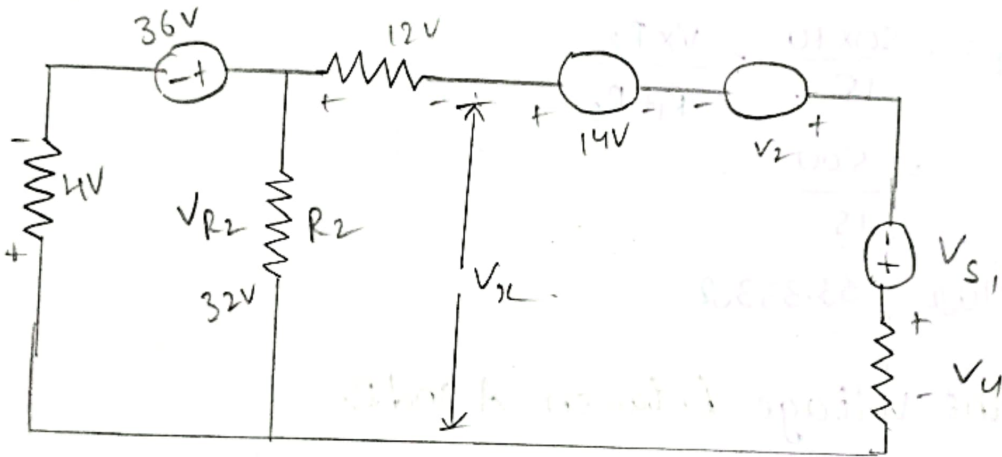
$V = IR$

$I = \frac{V}{R}$
 $= \frac{-4}{10}$

$I_x = -0.4A$



8) Find V_{R_2} , V_x in the circuit.



Sol: Apply KVL in loop ①

$-4 + 36 - V_{R_2} = 0$

$32 = V_{R_2}$

$V = IR$

$V_{R_2} - 12V - 14V - V_x = 0$

$32 - 12 - 14 = V_x$

$V_x = 6V$

9.) Find V_x in the circuit.

Sol: KVL for loop 1

$60V - 5(8) - 10I = 0$

$$60 - 40 = 10I$$

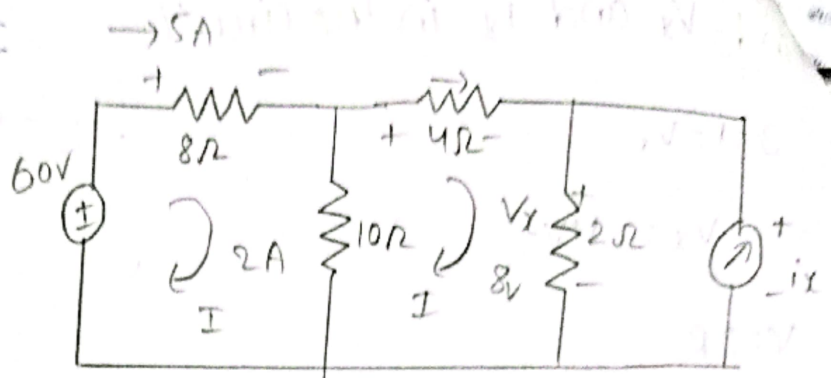
$$I = 2A$$

KVL for loop ②

$$10(2) - 3(4) - V_x = 0$$

$$20 - 12 = V_x$$

$$V_x = 8V$$



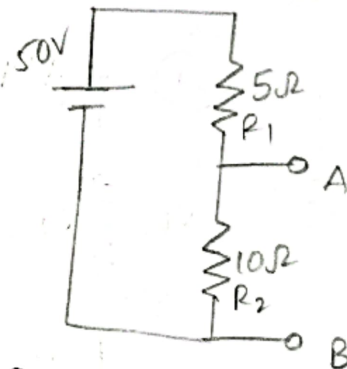
10.) Find the voltage across 10Ω resistor.

Sol:-

$$R_{10\Omega} = \frac{50 \times 10}{15} = \frac{V_x R_2}{R_1 + R_2}$$

$$= \frac{500}{15}$$

$$R_{10\Omega} = 33.333\Omega$$



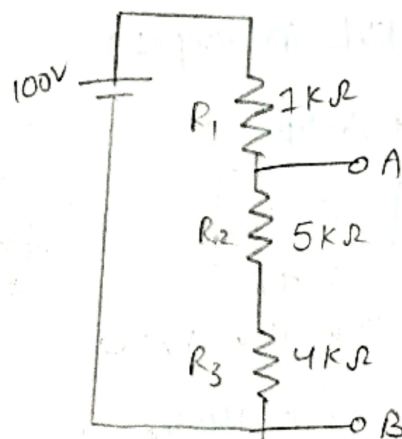
11.) Find the voltage between A and B.

Sol:-

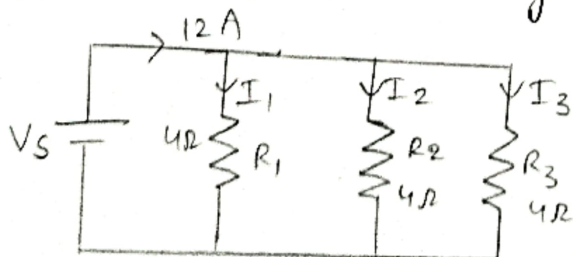
$$V_{AB} = \frac{V_x (R_2 + R_3)}{R_1 + R_2 + R_3}$$

$$= \frac{100 \times 9}{10}$$

$$V_{AB} = 90V$$



12.) Determine the current through each resistor in the circuit.

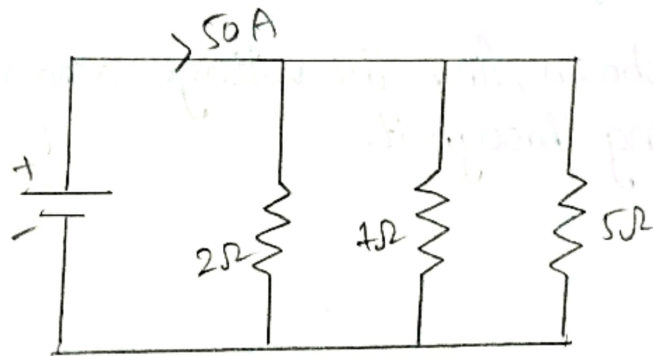


$$I_1 = \frac{I \cdot \frac{R_1 R_2}{R_2 + R_1}}{R_1 + R_2} = \frac{12 \times \frac{4 \times 4}{4+4}}{4+2} = \frac{24}{6} = 4A$$

$$I_2 = \frac{I \cdot \frac{R_2 R_3}{R_2 + R_3}}{R_2 + R_3} = 4A$$

$$I_3 = 4A$$

13.) Determine the currents in all the resistors in the given circuit.



$$R_{T1} = \frac{R_2 \times R_3}{R_2 + R_3} = \frac{5}{6} = 0.833$$

$$R_{T2} = \frac{R_1 \times R_3}{R_1 + R_3} = \frac{10}{7} = 1.429$$

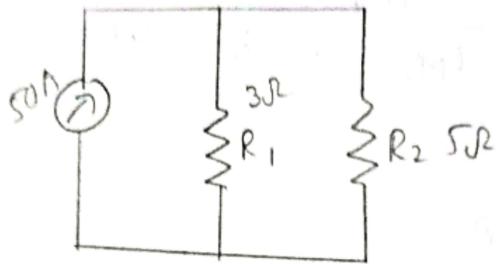
$$I_1 = \frac{50 \times 0.833}{2.833} = 14.702A$$

$$I_2 = \frac{50 \times 1.429}{1.1429} = 29.42A$$

$$R_{T3} = \frac{R_1 \times R_2}{R_1 + R_2} = \frac{2}{3} = 0.67$$

$$I_3 = \frac{50 \times 0.67}{5.67} = \frac{33.5}{5.67} = 5.91A$$

14.) Determine the current in each Resistor in the given circuit.

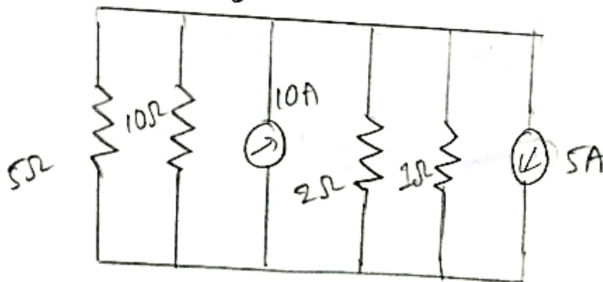


Sol:

$$I_1 = \frac{I \times R_2}{R_1 + R_2} = \frac{50 \times 5}{8} = \frac{250}{8} = 31.25 \text{ A}$$

$$I_2 = \frac{50 \times 3}{8} = \frac{150}{8} = 18.75 \text{ A}$$

15.) For the circuit shown, find the voltage across 10Ω resistor & the current passing through it.



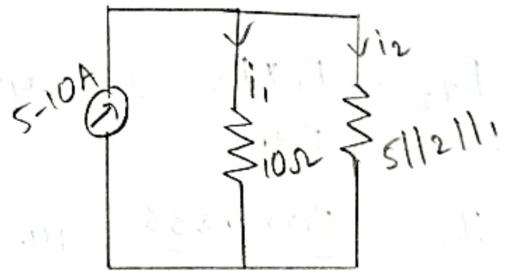
Sol:

$$I_{10\Omega} = \frac{0.588 \times 5}{10.588}$$

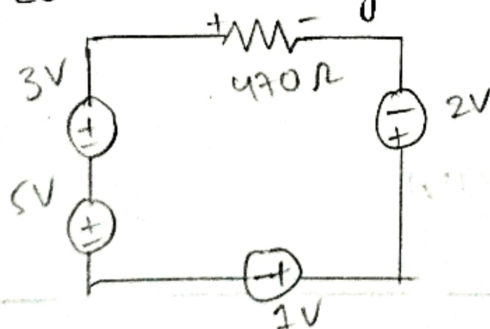
$$I_{10\Omega} = 0.278 \text{ A}$$

$$V_{10\Omega} = I_{10\Omega} (10\Omega)$$

$$V_{10\Omega} = 2.78 \text{ V}$$



16.) Find the current through 470Ω Resistor.



Sol:- Let I be the current flowing in 470Ω Resistor.

$$V = 5 + 3 - 470I + 2 - 1$$

$$= 9 - 470I$$

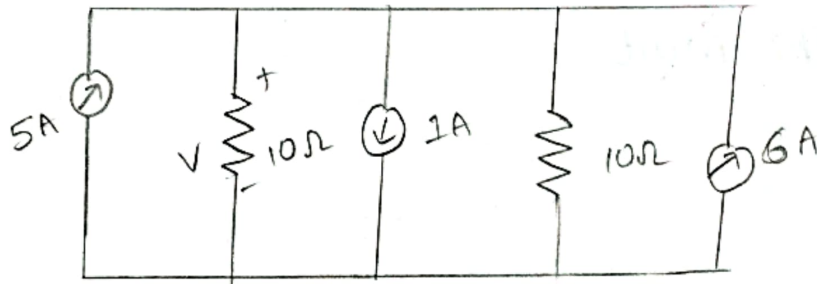
$$9 - 470I = 0$$

$$9 = 470I$$

$$I = 0.01915$$

$$I = 19.15\text{mA}$$

17.) Determine 'V' in the circuit.



Sol:- $I = 10\text{ A}$

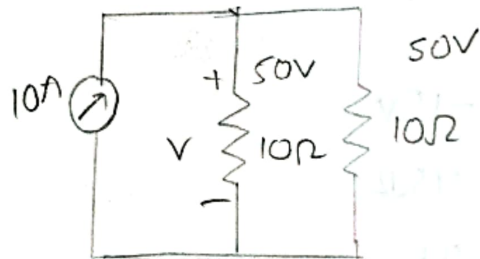
$$I_{10\Omega} = \frac{10 \times 10}{20}$$

$$= 5\text{ A}$$

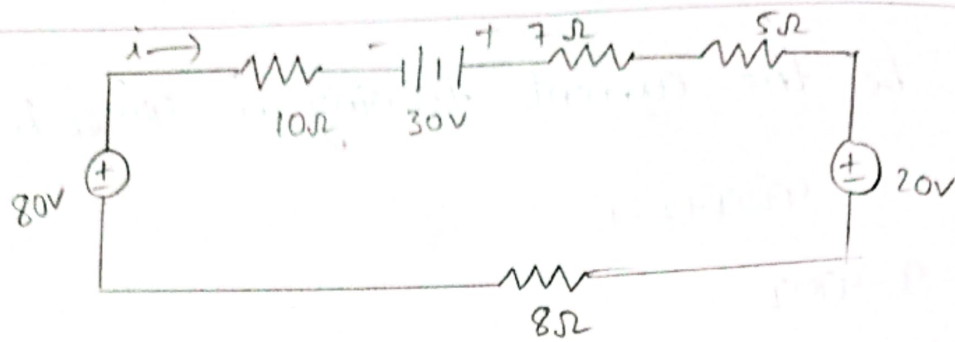
$$V = IR$$

$$V = 5 \times 10$$

$$\boxed{V = 50\text{V}}$$



18.) Find the current 'I' in the circuit & the power delivered by 80V source, use Resistance & source combinations.



$$V = 90V$$

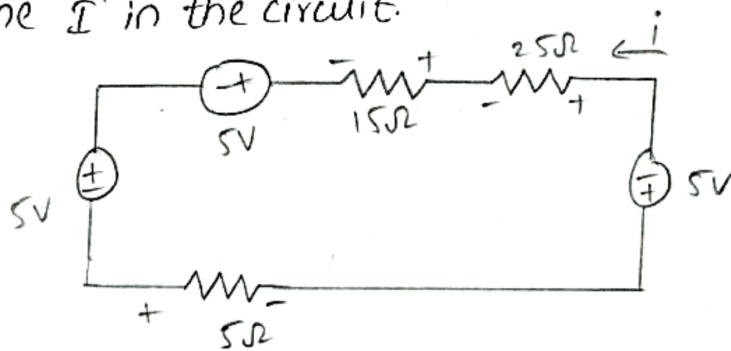
$$I = ?$$

$$R = 30\Omega$$

$$i = \frac{90}{30} = 3A$$

$$P_{(80V)} = Vi = 80(3) = 240 \text{ watts}$$

19.) Determine 'I' in the circuit.



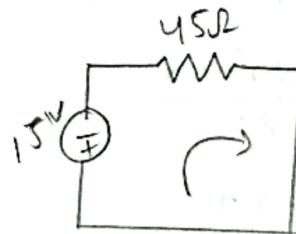
$$V = -15V$$

$$R = 45\Omega$$

$$V = IR$$

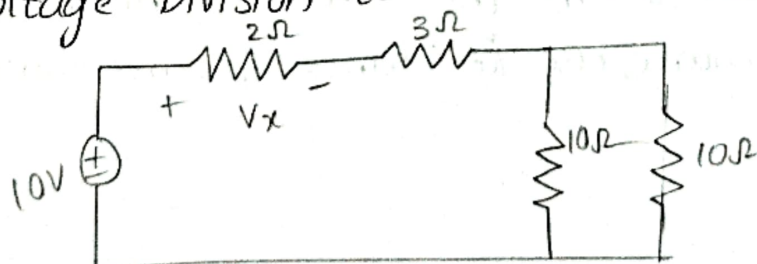
$$I = \frac{-15}{45} = -0.3333$$

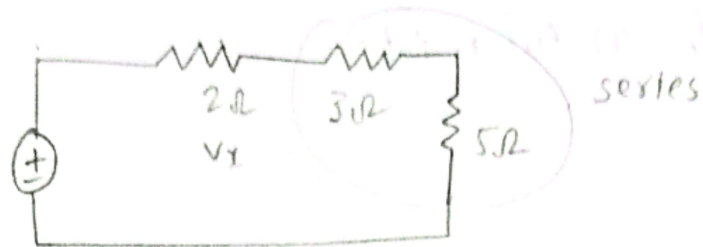
$$I = 0.3333$$



$$V = -15V$$

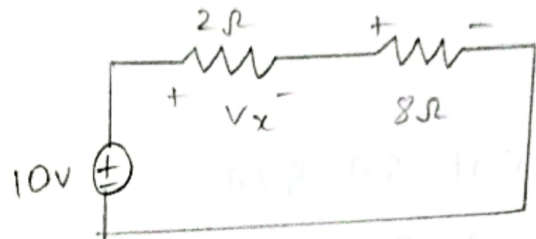
20.) Use voltage Division to determine V_x in the circuit.



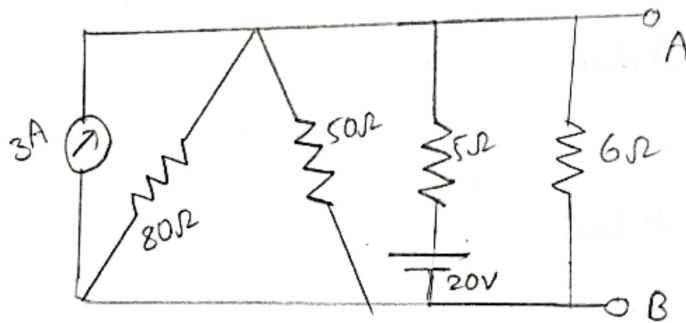


$$V_x = V_{2\Omega} = 10 \times \frac{2}{10}$$

$$V_x = 2V$$



21.) Replace the circuit with A & B with voltage source in series with a single resistor.



Sol: Convert a series combination of 20V, 5Ω into an equivalent circuit.

$$I = \frac{V}{R} = \frac{20}{5} = 4A$$

in parallel with 5Ω.

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}$$

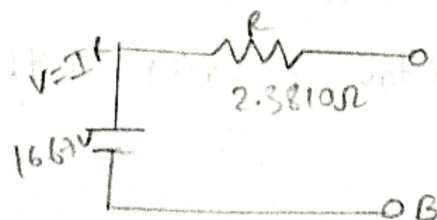
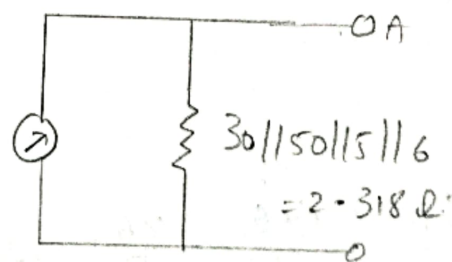
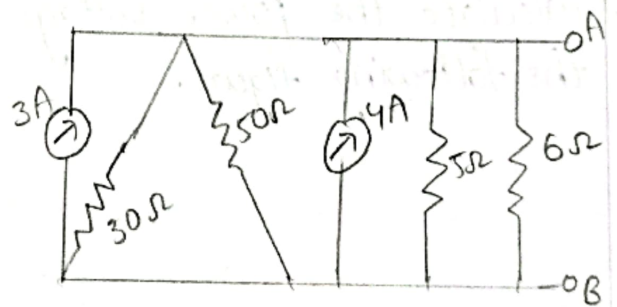
$$= \frac{1}{30} + \frac{1}{50} + \frac{1}{5} + \frac{1}{6}$$

$$R_T = 2.380\Omega$$

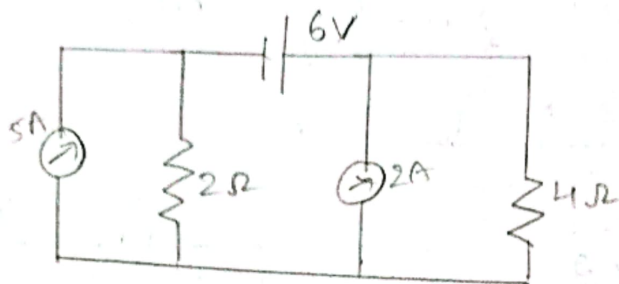
$$V = IR$$

$$= 7 \times 2.3810$$

$$= 16.67V$$



22) Find the current in 4Ω resistor.



Sol:- Convert 5A & 2A

$$V = IR$$

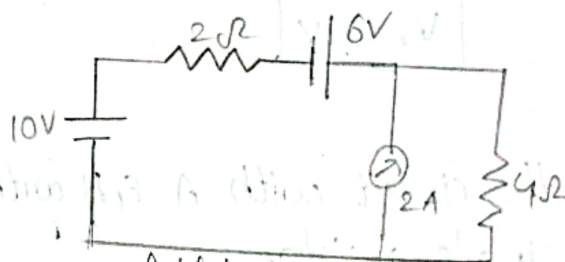
$$= 5 \times 2 = 10V$$

Combine 4V & 2Ω

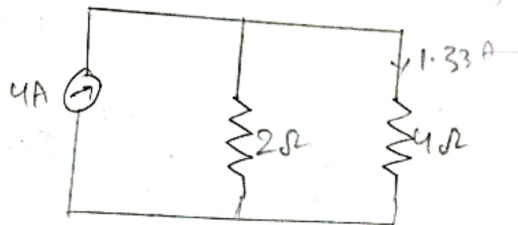
$$I = \frac{V}{R} = 2A, 2\Omega$$

$$I_{R_{4\Omega}} = 4 \times \frac{2}{6} = 1.33A$$

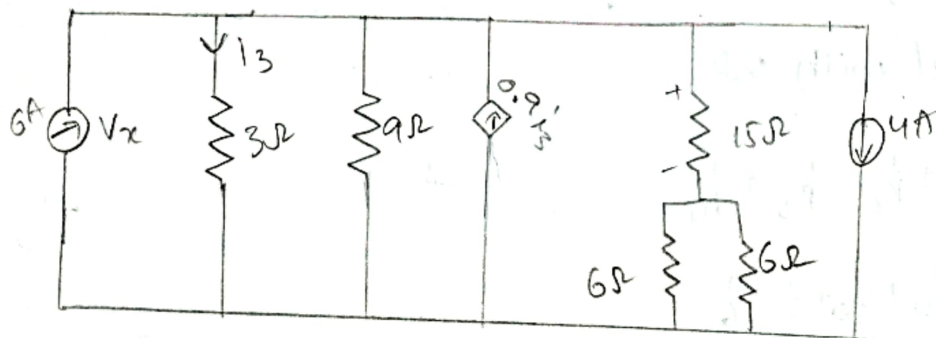
$$I_{R_{4\Omega}} = 1.33A$$



Add two voltage = 4V & then convert.



23) Calculate the power voltage source of the dependent source in the following figure.



$$\text{Sol:- } 6\Omega \parallel 6\Omega = \frac{6 \times 6}{6+6} = \frac{36}{12} = 3\Omega$$

3Ω resistor is series with 15Ω . $\Rightarrow 3+15 = 18\Omega$.

$$9 \parallel 18 \Rightarrow \frac{9 \times 18}{9 + 18} = 6 \Omega$$

Apply KCL at node A

$$2 + 0.9i_3 = i_3 + \frac{V_x}{6}$$

From the circuit $V_x = IR$

$$= i_3 \times 3$$

$$= 3i_3$$

$$\Rightarrow 2 + 0.9i_3 = i_3 + \frac{3i_3}{6}$$

$$2 = i_3 + \frac{3i_3}{6} - 0.9i_3$$

$$i_3 = \frac{2}{6}$$

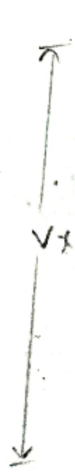
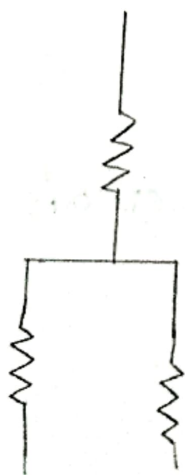
$$i_3 = 3.33$$

$$V_x = 3i_3 = 3 \times 3.33 = 9.99 \text{ V}$$

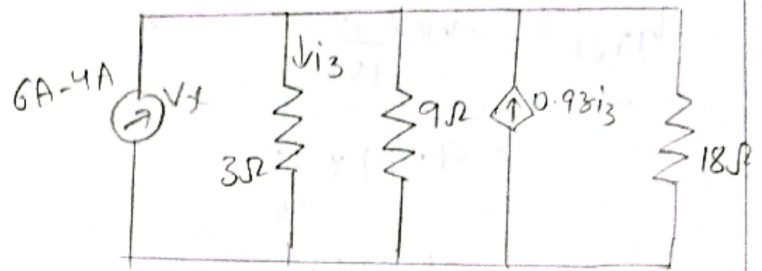
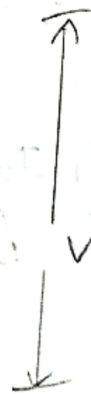
$$P = V \cdot i = 9.99 \times 0.9i_3 = 9.99 \times 0.9 \times 3.33$$

$$= 29.94003 \text{ Watts}$$

Q4) Calculate power dissipated in 15Ω Resistor.



$$\frac{6 \times 6}{6 + 6} = \frac{36}{12} = 3 \Omega$$



Sol:-

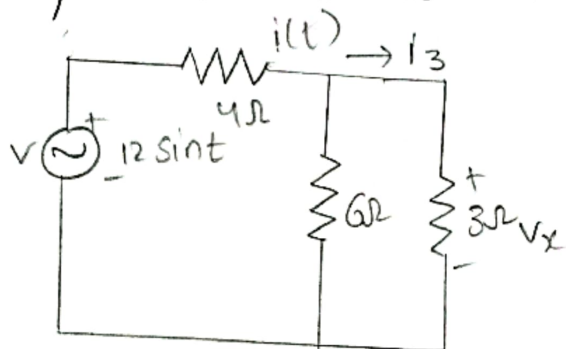
$$V_{15\Omega} = V_s \times \frac{15}{15+3}$$

$$= 9.99 \times \frac{15}{18}$$

$$= 8.325V$$

$$P_{15\Omega} = V_i^2 = V \cdot \frac{V}{R} = \frac{V^2}{R} = \frac{(8.325)^2}{15} = 4.63 \text{ Watts.}$$

25) Write an expression for the current through 3Ω resistor.



Sol:-

$$I = \frac{12 \sin t}{(6||3)+4}$$

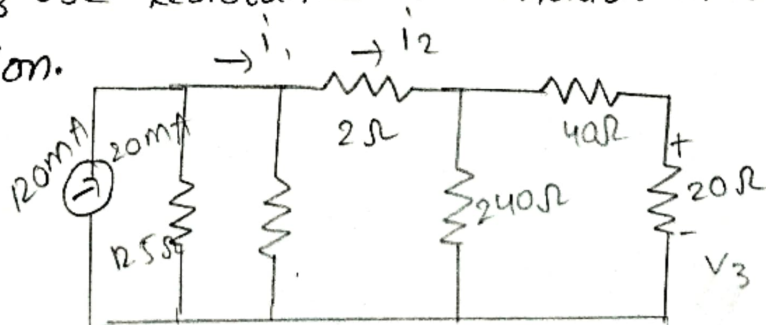
$$I = 2 \sin t$$

By using current division rule;

$$i_{3\Omega} = 2 \sin t \times \frac{6}{6+3} = 2 \sin t \times \frac{2}{3}$$

$$= \frac{4}{3} \sin t$$

26) Find I_1, I_2 & V_3 . Use Resistance combination methods & current division.

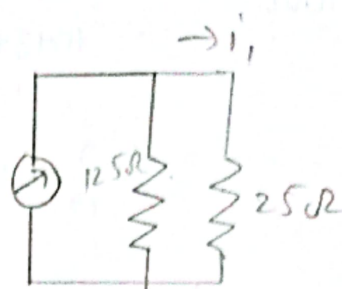


$$i_1 \Rightarrow \text{step (1)} : 40 + 20 = 60 \Omega$$

$$(2) : 60 \parallel 240 = \frac{60 \times 240}{60 + 240}$$

$$(3) : 48 + 2 = 50 \Omega$$

$$(4) : 50 \parallel 50 = \frac{50 \times 50}{50 + 50} = 25 \Omega$$



$$i_1 = 120 \text{mA} \times \frac{125}{125 + 25}$$

$$i_1 = 100 \text{mA}$$

$$i_2 \Rightarrow \text{step (1)}$$

$$i_2 = 100 \text{mA} \times \frac{50}{50 + 50}$$

$$= 50 \text{mA}$$

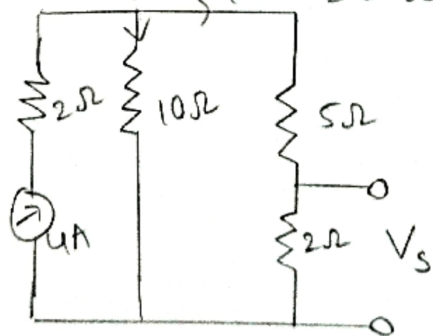
$$V_3 \Rightarrow I_{20\Omega} \times (20\Omega)$$

$$i_{20} = 50 \times \frac{240}{40 + 240 + 20}$$

$$= \frac{50 \times 240}{300} = 40 \text{mA}$$

$$\Rightarrow V_3 = 40 \text{mA} \times 20 \Omega = 0.8 \text{V}$$

27.) Determine the current in 10Ω resistor. Find V_s in the circuit.



$$I_{10\Omega} = 4A \times \frac{7}{10+2+5}$$

$$= 4 \times \frac{7}{17} = 1.65A$$

$$R_{eq} = \frac{1}{\frac{1}{2} + \frac{1}{10} + \frac{1}{5}}$$

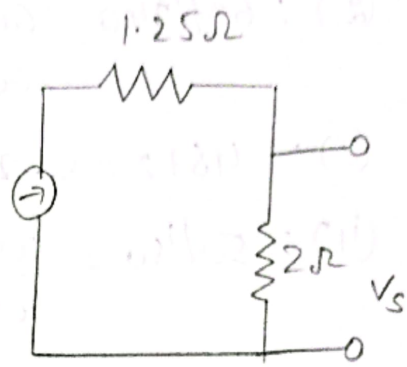
$$= \frac{10 \times 5 + 2 \times 5 + 2 \times 10}{2 \times 10 \times 5}$$

$$= \frac{50 + 10 + 20}{100} = 1.25$$

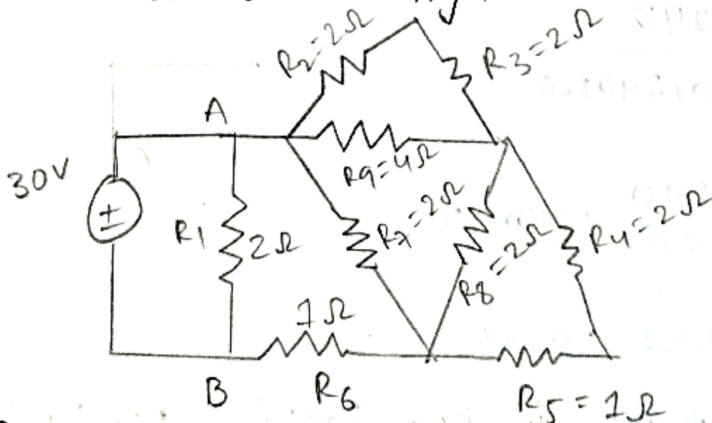
$$V = IR$$

$$V = 4 \times 2$$

$$V = 8V$$



Q8.) Determine the current delivered by the source in the circuit shown in figure.

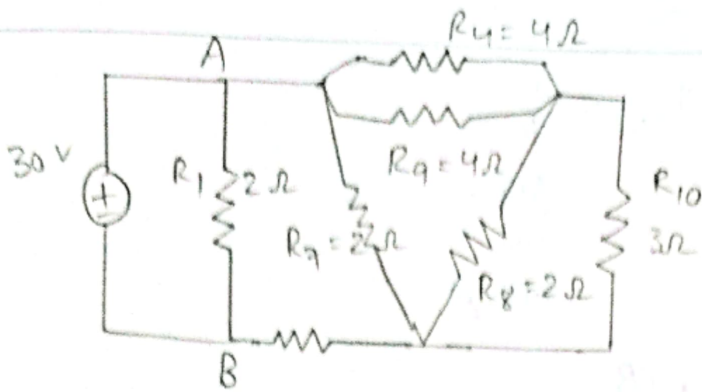


Sol: (1) $R_5 R_4 \rightarrow$ series

$$R_5 + R_4 = 3\Omega$$

(2) $R_2, R_3 \rightarrow$ series

$$R_2 + R_3 = 4\Omega$$



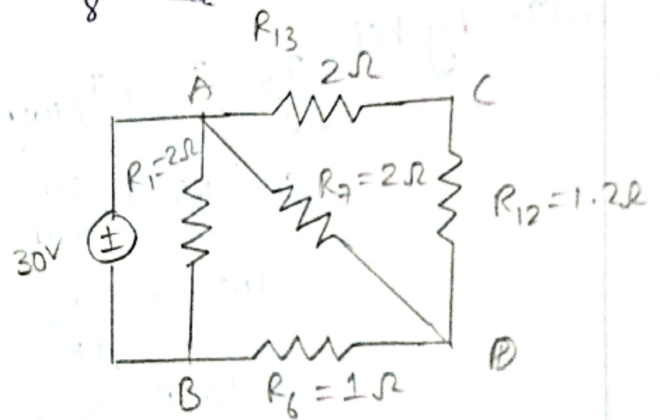
③ R_8 & R_{10} (Parallel) $= \frac{2 \times 3}{2 + 3} = \frac{6}{5} = 1.2 \Omega$

④ R_9 & R_{11} (Parallel) $R_{13} = \frac{4 \times 4}{4 + 4} = \frac{16}{8} = 2 \Omega$

⑤ R_{13}, R_{12} (Series)

$= 1.2 + 2$
 $= 3.2 \Omega$

R_1, R_6 (series) $= 2 + 1 = 3 \Omega$

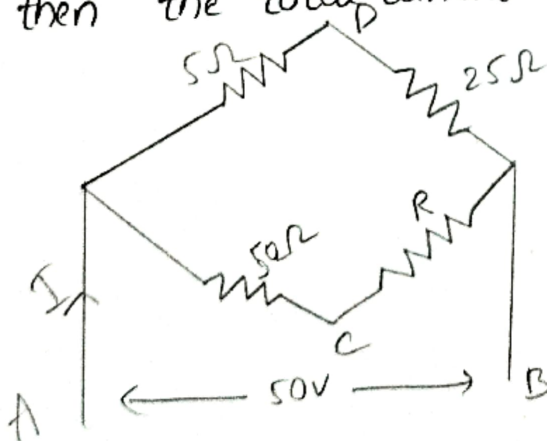


⑥ $3.2 \Omega \parallel R_7 = \frac{3.2 \times 2}{2 + 3.2} = 1.23 \Omega$

⑦ $1.23 + R_6 = 1.23 + 1 = 2.23 \Omega$

⑧ $2.23 \parallel 2 = \frac{2.23 \times 2}{2.23 + 2} = 1.05 \Omega$

29.) Determine the value of Resistance R & current in each branch; then the total current taken by the circuit is 6A.



Sol: The current in ABD $I_{30\Omega} = \frac{V}{R}$

$$= \frac{50}{30}$$

$$= 1.66 \text{ A}$$

The current in Branch ACB

$$I_{(10+R)} = \frac{V}{R}$$

$$= \frac{50}{10+R}$$

work: by KCL

$$I_7 = I_{30} + I_{(10+R)}$$

$$6 \text{ A} = 1.66 + \frac{50}{10+R}$$

$$4.34 = \frac{50}{10+R}$$

$$10+R = \frac{50}{4.34}$$

$$R = \frac{50}{4.34} - 10$$

$$R = 1.52 \Omega$$

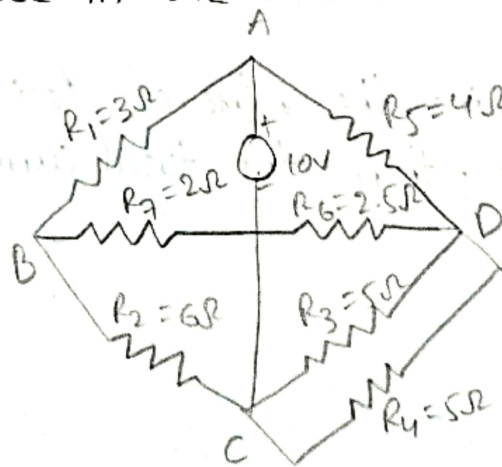
30) Find the power delivered by source in the circuit:

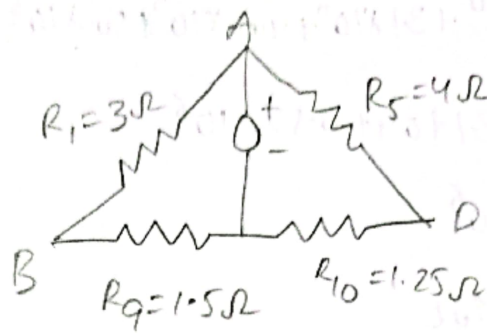
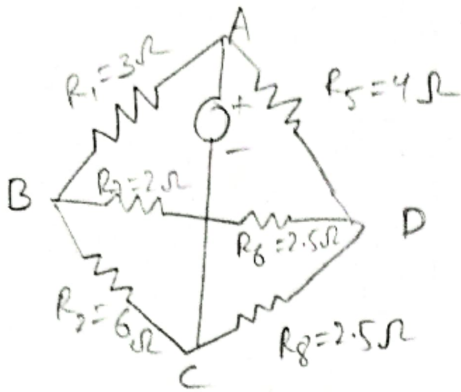
Sol: $R_8 \Rightarrow R_3 \parallel R_4$

$$= \frac{5 \times 5}{5+5} = 2.5 \Omega$$

$$R_9 \Rightarrow R_7 \parallel R_2 = \frac{2 \times 6}{2+6} = 1.5 \Omega$$

$$R_{10} \Rightarrow R_8 \parallel R_6 = \frac{2.5 \times 2.5}{2.5+2.5} = 1.25 \Omega$$





$$R_{11} \Rightarrow R_9 \parallel R_1 = 1.5 + 3 = 4.5 \Omega$$

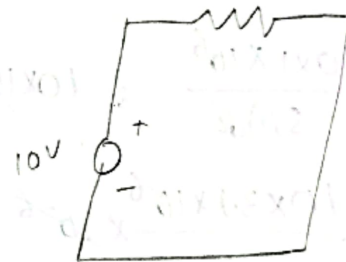
$$R_{12} \Rightarrow R_{10} \parallel R_5 = 4 + 1.25 = 5.25 \Omega$$

$$R_{13} \Rightarrow R_{11} \parallel R_{12} = \frac{4.5 \times 5.25}{4.5 + 5.25} = \frac{23.625}{9.75} = 2.42 \Omega$$

$$R_{13} = 2.42 \Omega$$

$$P = \frac{V^2}{R} = \frac{100}{2.42}$$

$$P = 41.322 \text{ watts}$$



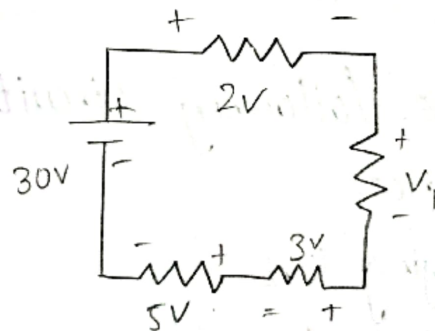
31) Determine the unknown voltage drop V_1 in the following circuit.

By KCL;

$$30 = -2 - V_1 - 3 - 5$$

$$V_1 = 30 + 10$$

$$V_1 = 40V$$



32) What is the current in the following circuit & determine voltage across each resistor.

Sol:- let i be the current

$$R_{eq} = 1 \times 10^6 + 3.1 \times 10^6 + 400 \times 10^3 + 500 \times 10^3$$

$$= (1 + 3.1 + 0.4 + 0.5) \times 10^6$$

$$= 5 \times 10^6$$

$$R_{eq} = 5 \text{ M}\Omega$$

$$\Rightarrow V = IR$$

$$I = \frac{V}{R} = \frac{10}{5} \times 10^{-6}$$

$$= 0.2 \times 10^{-5}$$

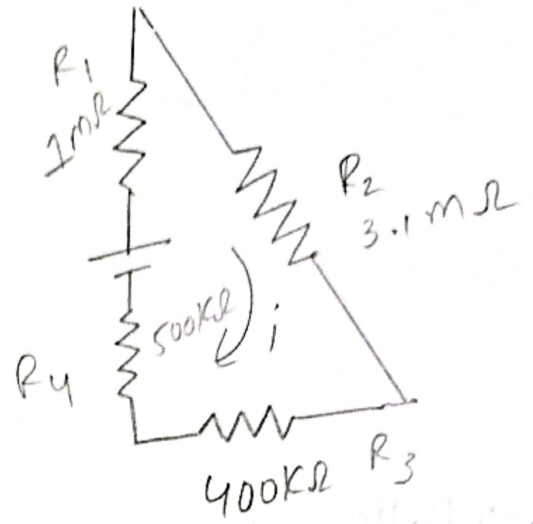
$$\boxed{I = 2 \mu\text{A}}$$

$$V_{R_1} = \frac{10 \times 1 \times 10^6}{5 \text{ M}\Omega} = 10 \times 10^6 \times 0.2 \times 10^{-6} = 2 \text{ V}$$

$$V_{R_2} = \frac{10 \times 3.1 \times 10^6}{5} \times 10^{-6} = 3.1 \times 0.2 = 6.2 \text{ V}$$

$$V_{R_3} = 10 \times 0.4 \times 10^6 \times 10^{-6} \times 0.2 = 0.8 \text{ V}$$

$$V_{R_4} = 10 \times 0.5 \times 10^6 \times 10^{-6} \times 0.2 = 1 \text{ V}$$



33) In the following circuit find i & voltage across 13Ω Resistance.

Sol:- By Applying KVL

$$= 230i - 2i + 100 - 8i - 40 = 0$$

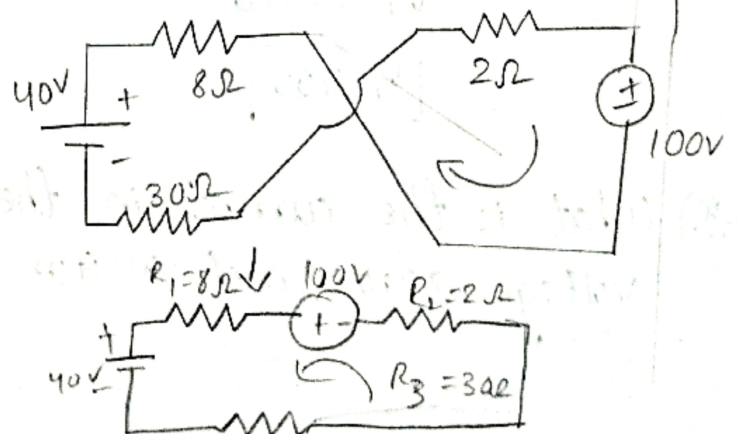
$$-40i = -60$$

$$\boxed{i = 1.5 \text{ A}}$$

By ohm's law; $V = IR$

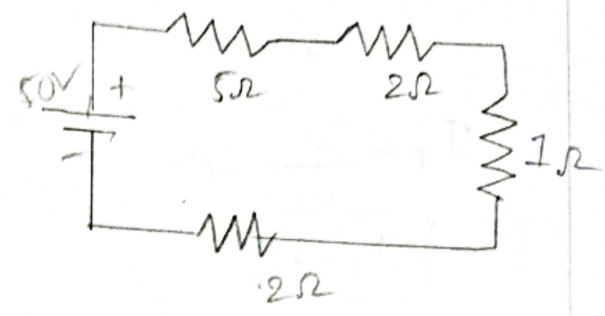
$$= 1.5 \times 30 = 45 \text{ V}$$

$$\boxed{V = 45 \text{ V}}$$



i) Determine the total amount power in the circuit. Find the power absorbed by each resistor.

$$P_T = \frac{V_T^2}{R_{eq}} = \frac{50^2}{5+2+1+2}$$



$$[\because P = Vi] = \frac{2500}{10} = 250 \text{ watts}$$

$$P_{5\Omega} = 25 \times 5 = 1.25 \text{ W}$$

$$P_{2\Omega} = 4 \times 5 = 20 \text{ W}$$

$$P_{1\Omega} = 1 \times 5 = 5 \text{ W}$$

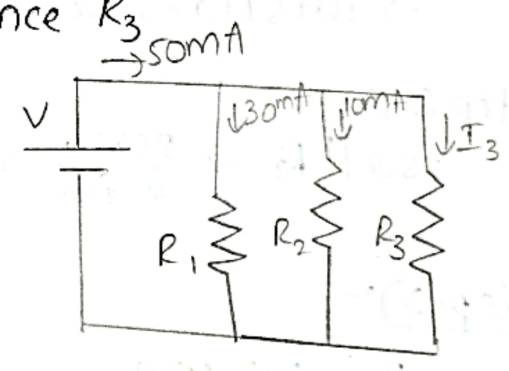
$$P_{2\Omega} = 4 \times 5 = 20 \text{ W}$$

35.) Determine current through resistance R_3

Sol:- By KCL;

$$50 = 30 + 10 + I_3$$

$$I_3 = 10 \text{ mA}$$

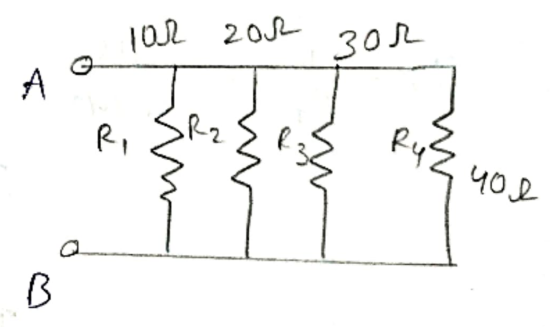


36.) Determine the parallel resistance b/w A & B of the circuit

$$\frac{1}{R_T} = \frac{1}{10} + \frac{1}{20} + \frac{1}{30} + \frac{1}{10}$$

$$\frac{1}{R_T} = 0.7$$

$$R_T = 1.43$$



37.) Determine the current through Resistor R_3 .

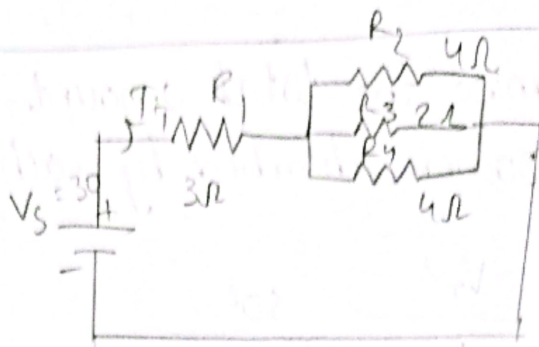
Sol:-

$$R_T = \frac{1}{\frac{1}{4} + \frac{1}{2} + \frac{1}{4}} + 5$$

$$= 1 + 5 = 6\Omega$$

$$I_T = \frac{30}{6} = 5A.$$

$$I_T = 5A.$$

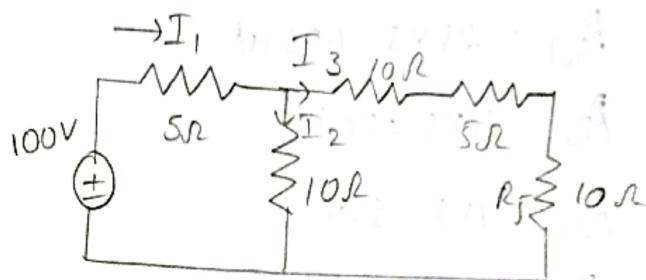


38) Find the current I_1, I_2, I_3 .

Sol:- Step (1):-

R_3, R_4 & R_5 are in series

$$\Rightarrow 10 + 5 + 10 = 25\Omega.$$



Step (2):-

$$25\Omega \parallel R_2 \Rightarrow \frac{25 \times 10}{25 + 10} = \frac{250}{35} = 7.142\Omega$$

Step (3):-

$$R_T = 5 + 7.142\Omega$$

$$= 12.142\Omega$$

$$I_T = \frac{V}{R_T} = \frac{100}{12.142} = 8.237A = I_1$$

$$I_2 = 8.237 \times \frac{10 + 10 + 5}{10 + 10 + 5 + 10} = 5.88A$$

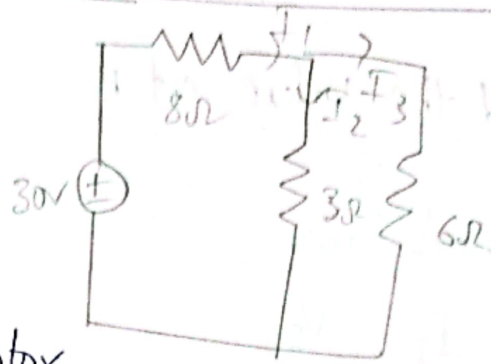
$$I_3 = I_1 - I_2 = 2.36A.$$

39.) Find the currents and voltages in the given circuit.

Sol:-

step 1) - $3\Omega // 6\Omega$

$$= \frac{3 \times 6}{3+6} = 2\Omega$$



step 2) - 8Ω is series with 2Ω resistor

$$8+2=10\Omega$$

$$I_1 = \frac{30}{10} = 3A$$

$$[-I_1 = I_2 + I_3]$$

$$I_2 = 3 \times \frac{6}{3+6} = 2A$$

$$I_3 = I_1 - I_2 = 1A$$

$$V_{8\Omega} = I_1 R = 3 \times 8 = 24V$$

$$V_{3\Omega} = 2 \times 3 = 6V$$

$$V_{6\Omega} = 1 \times 6 = 6V$$

10) Find the current supplied by the source.

soln step 1) - $\frac{2 \times 8}{12+8} = 4.8\Omega$

$$\frac{6 \times 3}{6+3} = \frac{18}{9} = 2\Omega$$



step 2) - $4.8 + 5 = 9.8\Omega$

$$= \frac{9.8 \times 2}{9.8+2} = 1.661\Omega$$

step 3) - $2 + 1.661\Omega$

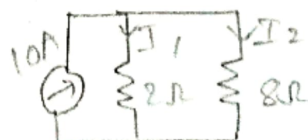
$$= 3.661\Omega$$

$$I_T = \frac{50}{3.661} = 13.66A$$

4) Find I_1 & I_2

soln $I_1 = 10 \times \frac{8}{8+2} = 8A$

$$I_2 = 10 \times \frac{2}{8+2} = 2A$$



42) Find the value of R.

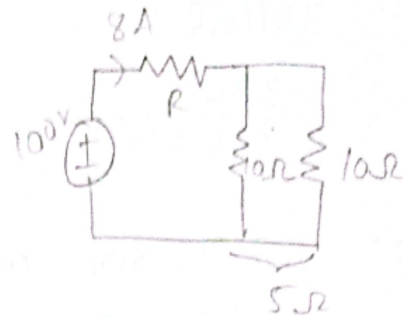
Sol: By Ohm's law;

$$I_T = \frac{V_s}{R_{eq}}$$

$$8 = \frac{100}{R+5}$$

$$R+5\Omega = 12.5$$

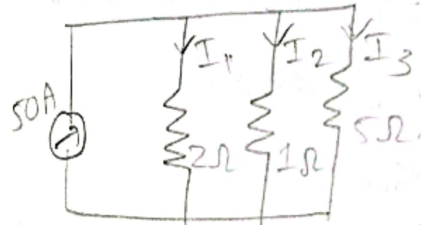
$$R = 7.5\Omega$$



43) Determine the current in all three resistors in the circuit.

Sol: KCL;

$$50 = I_1 + I_2 + I_3$$



let us assume that at point A the voltage is 'V'.

$$50 = \frac{V}{2} + \frac{V}{1} + \frac{V}{5}$$

$$50 = V \left[\frac{1}{2} + 1 + \frac{1}{5} \right]$$

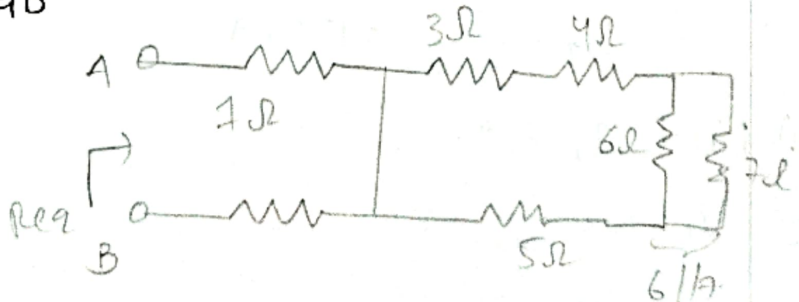
$$V = 29.41V$$

$$I_1 = I_{2\Omega} = \frac{V}{2} = \frac{29.41}{2} = 14.7A$$

$$I_2 = I_{1\Omega} = \frac{V}{1} = 29.41A$$

$$I_3 = I_{5\Omega} = \frac{V}{5} = \frac{29.41}{5} = 5.88A$$

44) Find Req between A & B



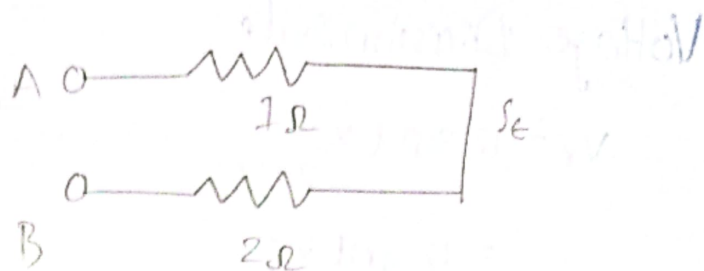
$$R_3 = 6 \parallel 7 = \frac{6 \times 7}{6+7} = 3.23 \Omega$$

In series

$$R_9 = 3 + 4 + 5 + 3.23 \\ = 15.23 \Omega$$

Because of short circuit the parallel resistance is to be neglected.

$$R_{eq} = 1 + 2 \\ R_{eq} = 3 \Omega$$



15.) Find all branch currents & voltages across all resistors.

$$R_T = 2.5 + 2.5 = 5 \Omega$$

$$I_T = \frac{10}{5} = 2 \text{ A}$$

$$I_3 = 2 \times \frac{5}{2+3+5} = 2 \times \frac{5}{10} = 1 \text{ A}$$

A + 'A', KCL;

$$I_1 = I_2 + I_3$$

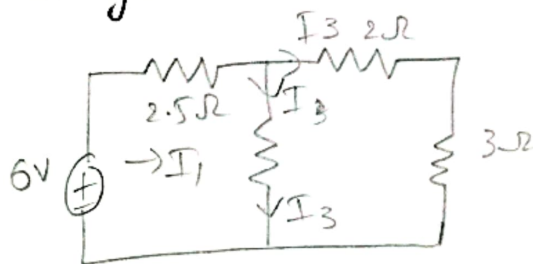
$$I_2 = 1 \text{ A}$$

$$V_{2.5 \Omega} = I_1(2.5) = 2 \times 2.5 = 5 \text{ V}$$

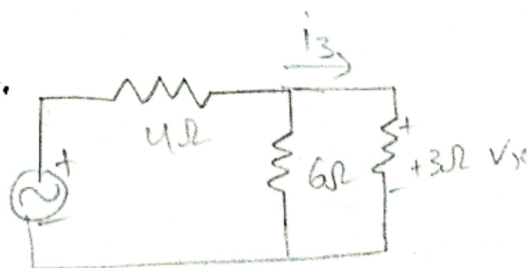
$$V_{2 \Omega} = I_2(2) = 1 \times 2 = 2 \text{ V}$$

$$V_{5 \Omega} = I_3(5) = 1 \times 5 = 5 \text{ V}$$

$$V_{3 \Omega} = I_3(3) = 1 \times 3 = 3 \text{ V}$$



46.) Determine V_x in the circuit.

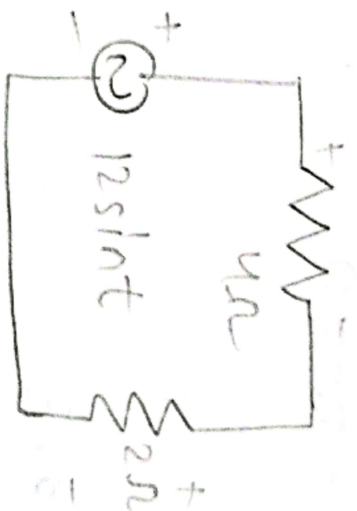


Sol:

Voltage Division rule

$$V_x = 12 \sin t \times \frac{2}{2+4}$$
$$= 12 \sin t \times \frac{2}{6}$$

∴ $V_x = 4 \sin t$ volts



∴ $V_x = 4 \sin t$ volts